
AP[®] Physics C: Electricity and Magnetism

Scoring Guidelines

Question 1: Mathematical Routines (MR)**10 points**

- A (i)** For a multistep derivation that includes the equation $\oint \vec{B} \cdot d\vec{\ell} = \mu_0 I_{\text{enc}}$ or an equivalent equation **Point A1**

Scoring Note: Vector notation and line integral notation are not required for this point to be earned.

For indicating that $\oint d\ell = 2\pi a$ **Point A2**

Scoring Note: Line integral notation is not required for this point to be earned.

For substituting $dA = 2\pi r dr$ and $J = Cr$ into $I = \int \vec{J} \cdot d\vec{A}$ **Point A3**

Scoring Note: Limits of integration are not required for this point to be earned.

For limits of integration from 0 to a for the current integral **Point A4**

(e.g., $I_{\text{enc}} = \int_0^a J dA$)

For a correct expression **Point A5**

(e.g., $B = \frac{\mu_0}{2\pi a} \left(\frac{2\pi Ca^3}{3} \right)$, $B = \frac{\mu_0 Ca^2}{3}$, or algebraic equivalent)

Example Response

$$\oint \vec{B} \cdot d\vec{\ell} = \mu_0 I_{\text{enc}}$$

$$B(2\pi a) = \mu_0 I_{\text{enc}}$$

$$B = \frac{\mu_0 I_{\text{enc}}}{2\pi a}$$

$$I = \int \vec{J} \cdot d\vec{A}$$

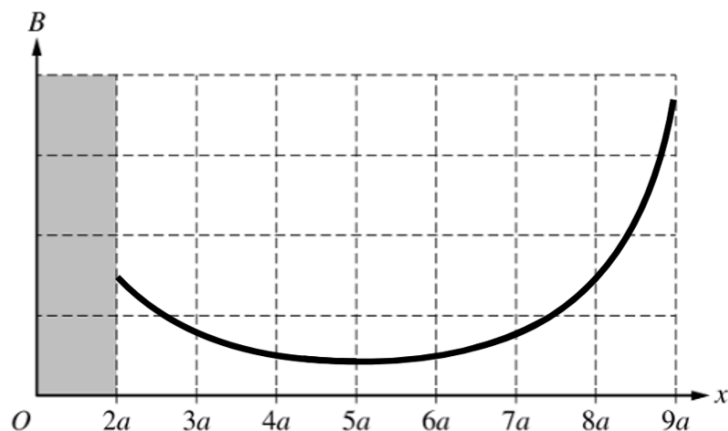
$$dA = 2\pi r dr$$

$$I_{\text{enc}} = \int_0^a Cr(2\pi r dr) = 2\pi C \int_0^a r^2 dr$$

$$I_{\text{enc}} = 2\pi C \left[\frac{r^3}{3} \right]_0^a = \frac{2\pi Ca^3}{3}$$

$$\therefore B = \frac{\mu_0}{2\pi a} \left(\frac{2\pi Ca^3}{3} \right) = \frac{\mu_0 Ca^2}{3}$$

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| (ii) | For a curve that has a minimum between $x = 4a$ and $x = 6a$ | Point A6 |
| | For a curve that is concave up everywhere with a value at $x = 9a$ that is greater than the value at $x = 2a$ | Point A7 |

Example Response

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| B | For a multistep derivation that includes $\vec{F} = q(\vec{v} \times \vec{B})$ | Point B1 |
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Scoring Note: Vector notation is not required for this point to be earned.

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| | For indicating that the net magnetic field (or net force) due to the currents in the wires is equal to the combination of the fields (or forces) from both wires | Point B2 |
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| | For a correct expression (e.g., $F = \frac{\mu_0 I_0 Q v}{5\pi a}$) | Point B3 |
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Example Response

$$\oint \vec{B} \cdot d\vec{\ell} = \mu_0 I_{\text{enc}}$$

Wire S

$$B_S(2\pi(5a)) = \mu_0 I_0$$

$$B_S = \frac{\mu_0 I_0}{10\pi a}$$

Wire T

$$B_T(2\pi(10a - 5a)) = \mu_0 I_0$$

$$B_T = \frac{\mu_0 I_0}{10\pi a}$$

Net Magnetic Field

$$B = B_S + B_T = \frac{\mu_0 I_0}{10\pi a} + \frac{\mu_0 I_0}{10\pi a} = \frac{\mu_0 I_0}{5\pi a}$$

$$\vec{F} = q(\vec{v} \times \vec{B})$$

$$F = qvB$$

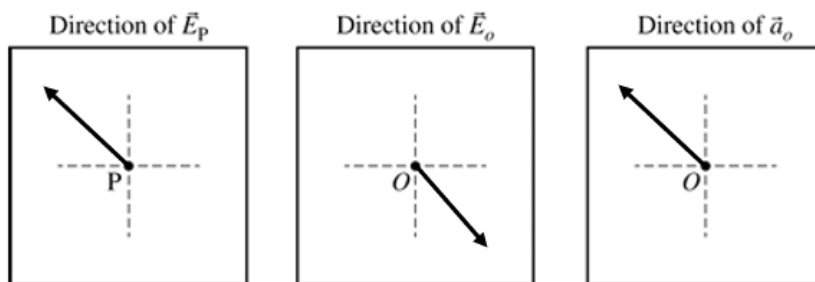
$$F = \frac{\mu_0 I_0 Q v}{5\pi a}$$

Question 2: Translation Between Representations (TBR)**12 points**

A For drawing an arrow that is up and to the left above the horizontal axis for the direction of $\vec{E}_P$ **Point A1**

For drawing an arrow that is down and to the right below the horizontal axis for the direction of $\vec{E}_O$ **Point A2**

For drawing an arrow for $\vec{a}_O$ that is directed opposite the arrow drawn for the direction of $\vec{E}_O$ **Point A3**

Example Response

B For a multistep derivation that includes the equation $\vec{E} = k \int \frac{dq}{r^2} \hat{r}$ **Point B1**

Scoring Note: Vector notation and unit vector notation are not required for this point to be earned.

For a substitution of a correct expression for dq that includes λ (e.g., $dq = \lambda dx$ or $dq = \lambda dy$) **Point B2**

For an attempt to solve the integral for a component of the net electric field that includes correct limits **Point B3**

For a correct vector addition of the derived electric fields for both rods resulting in an expression in terms of L , λ , and physical constants **Point B4**

Example Response

Determine magnitude E_T of the electric field due to Rod T at the origin.

$$\vec{E} = \frac{1}{4\pi\epsilon_0} \int \frac{dq}{r^2} \hat{r}$$

$$E_T = -k \int \left(\frac{1}{y^2} \right) dq$$

$$dq = \lambda dy$$

$$E_T = -k\lambda \int_L^{3L} \frac{dy}{y^2}$$

$$E_T = k\lambda \left(\frac{1}{y} \right) \Big|_L^{3L}$$

$$E_T = k\lambda \left(\frac{1}{3L} \right) - k\lambda \left(\frac{1}{L} \right) = -\frac{2}{3} \frac{k\lambda}{L}$$

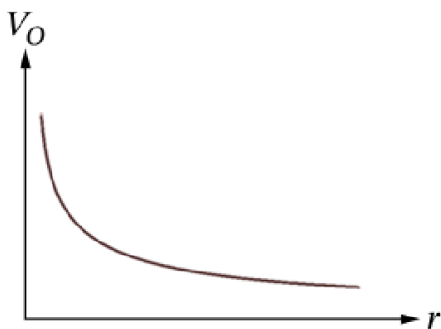
Magnitude E_S of the electric field due to Rod S is equal to E_T .

$$E_O = \sqrt{(E_S)^2 + (E_T)^2} = \sqrt{2(E_T)^2}$$

$$E_O = \sqrt{2 \left(\frac{2}{3} \frac{k\lambda}{L} \right)^2}$$

$$\therefore E_O = \frac{2\sqrt{2}}{3} \frac{k\lambda}{L}$$

C	For a curve that always decreases as r increases	Point C1
	For a curve with a slope whose absolute value always decreases as r increases	Point C2
	For a curve that approaches zero as r increases and approaches infinity as r decreases	Point C3

Example Response

D	For indicating that V_O is zero for all values of r	Point D1
	For a justification that indicates that the linear charge densities are equal in magnitude but opposite in sign and the rods are always the same distance from the origin	Point D2
	Example Response <i>The rods are identical in length but have equal and opposite linear charge densities. Electric potential is a scalar, and the electric potentials at the origin from the rods cancel because the rods are always the same distance from the origin. Therefore, $V_O = 0$.</i>	

Question 3: Experimental Design and Analysis (LAB)**10 points**

A (i) For indicating that the potential difference across the capacitor or the inductor is measured over time **Point A1**

(ii) For indicating a reasonable method of reducing experimental uncertainty **Point A2**
 Examples of acceptable responses may include the following:

- Different capacitors are used in subsequent trials
- Multiple trials are completed with the same capacitor

Example Response

Measure the potential difference across the capacitor as a function of time after the switch is closed for long enough to measure the period of oscillation. Repeat the procedure with different capacitors in subsequent trials.

B (i) For indicating appropriate quantities that can be graphed to determine L_1 , consistent with the response in part A (i), such as: **Point B1**

- T as a function of $\sqrt{C}$
- T^2 as a function of C
- Angular frequency ω as a function of $\sqrt{\frac{1}{C}}$

Scoring Note: Responses that include the reciprocals of the preceding examples, in addition to other equivalent graphs, also earn this point.

(ii) For correctly relating an appropriate feature of the graph to L_1 **Point B2**

Example Response

Graph T as a function of $2\pi\sqrt{C}$. The slope of the best-fit line is equal to $\sqrt{L_1}$.

C (i) For indicating appropriate quantities that can be graphed to determine L_2 , for example: **Point C1**

- $\Delta V_{\text{Battery}} - IR$ as a function of $\frac{dI}{dt}$
- ΔV_L as a function of $\frac{dI}{dt}$

Scoring Note: This point may be earned:

- If the vertical and horizontal variables are reversed
- For other equivalent graphs

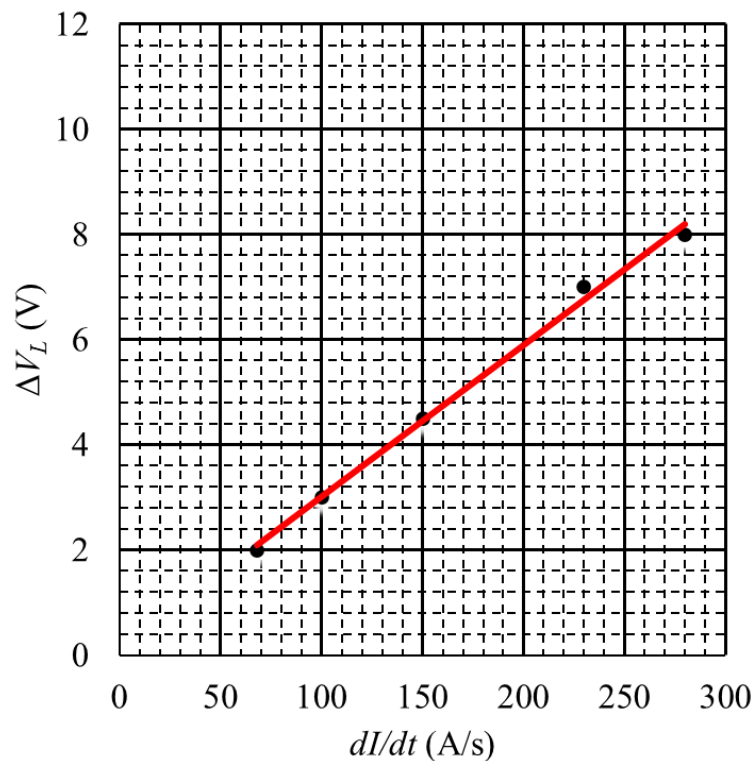
(ii) For labeling **both** axes (including units where appropriate) with a linear scale **Point C2**

For correctly plotting data points consistent with **one** of the following: **Point C3**

- The quantities indicated in part C (i)
- The quantities provided in the table

- (iii) For drawing a line or curve that approximates the trend of the plotted data

Point C4

Example Response

- D**
- For correctly relating the slope of the best-fit line of the graph to
- L_2

Point D1

For a value of L_2 that is within a range of 0.026 H to 0.032 H

Point D2

Example Response*Determine the Potential Difference Across the Inductor:*

$$\Delta V_{\text{Battery}} - \Delta V_R - \Delta V_L = 0$$

$$\Delta V_L = \Delta V_{\text{Battery}} - \Delta V_R$$

$$\Delta V_L = \Delta V_{\text{Battery}} - IR$$

Determine the Inductance of the Inductor:

$$|\Delta V_L| = L \frac{dI}{dt}$$

$$\text{slope} = L = \frac{\Delta(|\Delta V_L|)}{\Delta\left(\frac{dI}{dt}\right)}$$

$$\frac{\Delta(|\Delta V_L|)}{\Delta\left(\frac{dI}{dt}\right)} = \frac{(7.7 \text{ V}) - (5.3 \text{ V})}{(260 \text{ A/s}) - (180 \text{ A/s})}$$

$$\therefore L_2 = 0.03 \text{ H}$$

Question 4: Qualitative Quantitative Translation (QQT)**8 points**

A	For indicating that I is counterclockwise	Point A1
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	For indicating that the magnitude of the magnetic field is decreasing	Point A2
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	For indicating that the induced magnetic field will oppose the changing flux through the loop	Point A3
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Example Response

During the time interval, the magnetic field is directed in the $+z$ -direction and is decreasing in magnitude. To oppose this change in flux through the loop, the induced magnetic field must also be directed in the $+z$ -direction. Therefore, a counterclockwise current is induced in the loop.

B	For a multistep derivation that includes $\Phi_B = \int \vec{B} \cdot d\vec{A}$, $\varepsilon = -\frac{d\Phi_B}{dt}$, or $I = \frac{\Delta V}{R}$	Point B1
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Scoring Note: Vector notation is not required for this point to be earned.

	For substituting $B_0 \cos\left(2\pi \frac{t}{t_1}\right)$ for B into an equation for magnetic flux	Point B2
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	For a correct expression (e.g., $I = \frac{2\pi s^2 B_0}{t_1 R} \sin\left(2\pi \frac{t}{t_1}\right)$)	Point B3
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Scoring Note: Sign will not be considered when awarding this point.

Example Response

$$\Phi_B = \int \vec{B} \cdot d\vec{A}$$

$$\Phi_B = B_0 \cos\left(2\pi \frac{t}{t_1}\right) s^2$$

$$\varepsilon = -\frac{d\Phi_B}{dt}$$

$$\varepsilon = -B_0 s^2 \frac{d}{dt} \left(\cos\left(2\pi \frac{t}{t_1}\right) \right)$$

$$\varepsilon = \frac{2\pi s^2 B_0}{t_1} \sin\left(2\pi \frac{t}{t_1}\right)$$

$$I = \frac{\Delta V}{R} = \frac{\varepsilon}{R}$$

$$I = \frac{2\pi s^2 B_0}{t_1 R} \sin\left(2\pi \frac{t}{t_1}\right)$$

C	For indicating $I_2 > I_1$	Point C1
	For a justification that correctly references the functional dependence of the current on s and R in the expression derived in part B	Point C2
	Example Response <i>$I_2 > I_1$. The side length and the resistance of the loop doubles. The derivation in part B shows that the current is proportional to the square of the side length and inversely proportional to R, so the current increases.</i>	