2023



AP[°] **Statistics** Sample Student Responses and Scoring Commentary

Inside:

Free-Response Question 2

- \square Scoring Guidelines
- ☑ Student Samples
- **☑** Scoring Commentary

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Question 2: Focus on Sampling and Experimental Design

General Scoring Notes

- Each part of the question (indicated by a letter) is initially scored by determining if it meets the criteria for essentially correct (E), partially correct (P), or incorrect (I). The response is then categorized based on the scores assigned to each letter part and awarded an integer score between 0 and 4 (see the table at the end of the question).
- The model solution represents an ideal response to each part of the question, and the scoring criteria identify the specific components of the model solution that are used to determine the score.

Model Solution	Scoring
 (a) Experimental units: 60 driveways. Treatments: Concrete with fibers and concrete without fibers. Response variable: Rating of the severity of the cracks after one year, on a scale of 0 to 10. 	 Essentially correct (E) if the response satisfies the following three components: 1. Identifies the experimental units as the driveways 2. Identifies the treatments as concrete with fibers and concrete without fibers 3. Identifies the response variable as the rating of the severity of the cracks Partially correct (P) if the response satisfies only two of the three components. Incorrect (I) if the response does not meet the
Additional Notes	criteria for E or P.

- The number of experimental units is not necessary to satisfy component 1.
- The experimental units can be identified as "new homes needing driveways" to satisfy component 1.
- The phrases "on a scale of 0 to 10" and "after one year" are not required for component 3.
- Reasonable synonyms for "rating of the severity" such as "rating," "severity," or "on a scale of 0 to 10" are acceptable towards satisfying component 3.
- Identification of the response variable as a mean, or average, does not satisfy component 3.

	Model Solution	Scoring
(b)	Number the 60 driveways from 01 to 60. Using a random number generator, generate two-digit integers between 01 and 60. Ignore 00 and any number greater than 60 until 30 unique numbers are obtained. Assign the driveways with those 30 unique numbers to receive concrete with fibers and the remaining 30 driveways to receive concrete without fibers.	 Essentially correct (E) if the response satisfies the following two components: Describes how to correctly use a random number generator, or some other appropriate random process, to assign driveways that have been labeled 1 to 60 to concrete with fibers and concrete without fibers so that every possible random assignment is equally likely The random process results in an equal number of driveways assigned to the concrete with fibers and the concrete without fibers Partially correct (P) if the response describes how to implement a random process that satisfies only one of the two components. Incorrect (I) if the response does not meet the criteria for E or P.
Additi	onal Notes:	

• Examples of alternative random assignment processes that satisfy both component 1 and component 2 include:

- Put 60 equally sized slips of paper labeled from 1 to 60 into a hat, mix well, and randomly select 30 slips of paper out of the hat, sampling <u>without replacement</u>. Assign the driveways with the numbers on the 30 selected slips of paper to concrete with fibers and assign the remaining 30 driveways to concrete without fibers.
- Put 30 white marbles and 30 black marbles in an urn and mix well. Randomly select one marble from the urn. If the marble is white, assign the driveway with label 1 to concrete with fibers, otherwise assign the driveway with label 1 to concrete without fibers. Randomly select a marble from the remaining 59 marbles in the urn. If the marble is white, assign the driveway with label 2 to concrete with fibers, otherwise assign the driveway with label 2 to concrete without fibers. Continue this process of randomly selecting marbles from the urn without replacement until 30 driveways are assigned to concrete with fibers. The other 30 driveways are assigned to concrete without fibers.
- Spin a spinner with 60 equally sized sections numbered from 1 to 60, ignoring repeats, until 30 unique numbers are generated. Assign the driveways with those 30 numbers to concrete with fibers and assign the remaining 30 driveways to concrete without fibers.
- The following random assignment processes are examples that would satisfy component 2 but would not satisfy component 1.
 - An example that does not specify without replacement: Put 60 equally sized slips of paper labeled from 1 to 60 into a bowl, mix well, and randomly select one slip out of the bowl and record the number. Continue this process of randomly selecting slips until 30 numbers are recorded. Assign the driveways with the 30 recorded numbers to concrete with fibers and assign the remaining 30 driveways to concrete without fibers.

AP® Statistics 2023 Scoring Guidelines

- An example of a stopping rule with equal probabilities: Put 30 white marbles and 30 black marbles into an urn and mix well. Randomly select one marble from the urn. If the marble is white, assign the driveway with label 1 to concrete with fibers, otherwise assign the driveway with label 1 to concrete with fibers. Place the selected marble back into the urn, mix well, and randomly select a marble from the urn. If the marble is white, assign the driveway with label 2 to concrete with fibers, otherwise assign the driveway with label 2 to concrete with fibers, otherwise assign the driveway with label 2 to concrete with fibers. Continue this process of randomly selecting marbles from the urn with replacement until 30 driveways are assigned to concrete with fibers. The other 30 driveways are assigned to concrete without fibers.
- An example where not all outcomes are equally likely: Toss 60 fair coins and record the number of heads. Continue tossing the 60 coins, and ignoring zero, until 30 unique numbers are recorded. Assign the driveways with the 30 recorded numbers to concrete with fibers and assign the remaining 30 driveways to concrete without fibers.
- If there is not some type of labeling system (numbering the driveways), then component 1 is not satisfied.
- If it is not clear that the random assignment process allows every possible random assignment of driveways to type of concrete to be equally likely, then component 1 is not satisfied.
- If the response does not clearly indicate that random numbers are selected without using repeats, then component 1 is not satisfied.
- A response that only assigns driveways to groups and does not indicate how the groups correspond to concrete with fibers and concrete without fibers does not satisfy component 1.
- If a response describes two separate random assignment processes in detail (e.g., how to randomly assign number labels to driveways <u>and</u> how to randomly assign driveways to concrete type), score the combined random assignment process according to the two components.
- If the response describes two ways to make the same random assignment (e.g., how to randomly assign driveways to treatments), assign the score for the weaker random assignment process.

	Model Solution	Scoring
(c)	The results were statistically significant, and because the driveways were randomly assigned to either the concrete with the fibers or the concrete without the fibers, there is evidence the treatment (type of concrete) caused the response (rating of severity of cracks).	 Essentially correct (E) if the response satisfies the following two components: 1. The response indicates that random assignment enables the conclusion that type of concrete caused the rating of severity of the cracks 2. The explanation is in context of the problem Partially correct (P) if the response satisfies only component 1, <i>OR</i> the response indicates random assignment limits the effect of confounding variables in context. Incorrect (I) if the response does not meet the criteria for E or P.
Additi	onal Notes:	

- If the response also indicates an incorrect conclusion based on random assignment, such as generalization, representation of the population, reduction of bias, or reduction of variability, reduce the score from an E to a P or from a P to an I.
- Context includes either the treatment (concrete with fibers or concrete without fibers or "fibers") or the severity rating.

AP® Statistics 2023 Scoring Guidelines

Scoring for Question 2	Score
Complete Response	4
Three parts essentially correct	
Substantial Response	3
Two parts essentially correct and one part partially correct	
Developing Response	2
Two parts essentially correct and no part partially correct	
OR	
One part essentially correct and one or two parts partially correct	
OR	
Three parts partially correct	
Minimal Response	1
One part essentially correct and no part partially correct	
OR	
No part essentially correct and two parts partially correct	

Question 2

Begin your response to QUESTION 2 on this page.

Sample 2A

GO ON TO THE NEXT PAGE

Q5214/4

2. A developer wants to know whether adding fibers to concrete used in paving driveways will reduce the severity of cracking, because any driveway with severe cracks will have to be repaired by the developer. The developer conducts a completely randomized experiment with 60 new homes that need driveways. Thirty of the driveways will be randomly assigned to receive concrete that contains fibers, and the other 30 driveways will receive concrete that does not contain fibers. After one year, the developer will record the severity of cracks in each driveway on a scale of 0 to 10, with 0 representing not cracked at all and 10 representing severely cracked.

(a) Based on the information provided about the developer's experiment, identify each of the following.

· Experimental units

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The experimental units are the Go New driveways being paved • Treatments either recieving concrete with fibers or recieveing concrete · Response variable The severity of cracks on a driveway after one year on a scale from 0-10 (b) Describe an appropriate method the developer could use to randomly assign concrete that contains fibers and concrete that does not contain fibers to the 60 driveways. The developer should first assign each driveway a number 1-60. then the developer should use a RNG From 1-60 to select so numbers without reapeats. assign the houses who corresponding number was Selected by the vandom number generator to concrete containing fibers and assign the remaining 30 Houses to Concrete that doesn't contain fibers.

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Page 4

Question 2

Continue your response to QUESTION 2 on this page.

Suppose the developer finds that there is a statistically significant reduction in the mean severity of cracks in driveways using the concrete that contains fibers compared to the driveways using concrete that does not contain fibers.

(c) In terms of the developer's conclusion, what is the benefit of randomly assigning the driveways to either the concrete that contains fibers or the concrete that does not contain fibers?

The benefit of randomly assigning the two treatments (concrete with/without fibers) is so that the developer can conclude that the concrete with fibers is causing less driveway creacks than concrete without fibers. Concluding causation wouldn't be possible without the random assignment of the two treatments.

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Q5214/5

2 of 2

Page 5

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Question 2

Begin your response to QUESTION 2 on this page. 2. A developer wants to know whether adding fibers to concrete used in paving driveways will reduce the severity of cracking, because any driveway with severe cracks will have to be repaired by the developer. The developer conducts a completely randomized experiment with 60 new homes that need driveways. Thirty of the driveways will be randomly assigned to receive concrete that contains fibers, and the other 30 driveways will receive concrete that does not contain fibers. After one year, the developer will record the severity of cracks in each driveway on a scale of 0 to 10, with 0 representing not cracked at all and 10 representing severely cracked. (a) Based on the information provided about the developer's experiment, identify each of the following. Experimental units 60 homes in need of driveways The The concrete that contains fibers and the concrete • Response variable that doesn't Treatments The severity of cracks in each driveway (b) Describe an appropriate method the developer could use to randomly assign concrete that contains fibers and concrete that does not contain fibers to the 60 driveways. The developer could number each driveway from 1-60 and write each number on a slip of paper and place them in a hat. The developer would then draw 30 slips out of the hat and those driveways would receive the concrete that contains Fibers. The remaining 30 driveways would receive the concrete that doesn't contain fibers. GO ON TO THE NEXT PAGE. Unauthorized copying or reuse of this page is illegal. Page 4 Use a pencil or a pen with black or dark blue ink. Do NOT write your name. Do NOT write outside the box. Q5214/4

05214/5

Sample 2B

Question 2

Continue your response to QUESTION 2 on this page.

Suppose the developer finds that there is a statistically significant reduction in the mean severity of cracks in driveways using the concrete that contains fibers compared to the driveways using concrete that does not contain fibers.

(c) In terms of the developer's conclusion, what is the benefit of randomly assigning the driveways to either the concrete that contains fibers or the concrete that does not contain fibers?

The developer can infer cause and effect due to the random assignment of treatments (types of concrete) to the experimental units (driveways). The developer can conclude that using concrete with fibers for driveways like the ones in the experiment will reduce the severity of cracks in the driveways as opposed to using concrete without fibers. Unauthorized copying or reuse of this page is illegal. GO ON TO THE NEXT PAGE Page 5 Use a pencil or a pen with black or dark blue ink. Do NOT write your name. Do NOT write outside the box.

Question 2

Begin your response to **QUESTION 2** on this page. 2. A developer wants to know whether adding fibers to concrete used in paving driveways will reduce the severity of cracking, because any driveway with severe cracks will have to be repaired by the developer. The developer conducts a completely randomized experiment with 60 new homes that need driveways. Thirty of the driveways will be randomly assigned to receive concrete that contains fibers, and the other 30 driveways will receive concrete that does not contain fibers. After one year, the developer will record the severity of cracks in each driveway on a scale of 0 to 10, with 0 representing not cracked at all and 10 representing severely cracked. (a) Based on the information provided about the developer's experiment, identify each of the following. • Experimental units 60 homes that new diverses • Treatments Concrete with fibers, concrete w/o fibers Response variable Severity of cracking on a driveway (b) Describe an appropriate method the developer could use to randomly assign concrete that contains fibers and concrete that does not contain fibers to the 60 driveways. USING a rondom number generator we can first make the house 1-60 (save that). Then with the random generator we get 30 numbers from the list of 1-60 lie male. Those coo be asymptic to control with Fiber, we can then add the telet to Converce In Hhart fibers Unauthorized copying or reuse of this page is illegal. Page 4 GO ON TO THE NEXT PAGE. Use a pencil or a pen with black or dark blue ink. Do NOT write your name. Do NOT write outside the box. Q5214/4

Question 2 Continue your response to QUESTION 2 on this page. Suppose the developer finds that there is a statistically significant reduction in the mean severity of cracks in driveways using the concrete that contains fibers compared to the driveways using concrete that does not contain fibers. (c) In terms of the developer's conclusion, what is the benefit of randomly assigning the driveways to either the concrete that contains fibers or the concrete that does not contain fibers? The benefit of Ichdomity assings drive ways is to relive conforming. If the developer did not rendomly assign there could be a chance he assings the concre with fibers to the "worse's drive ways so he would have to reduc it. 1 46 15 1 211 1 (! . ! Same of Philips 1 91.1 Unauthorized copying or reuse of this page is illegal. Page 5 GO ON TO THE NEXT PAGE. Use a pencil or a pen with black or dark blue ink. Do NOT write your name. Do NOT write outside the box. 05214/5

Question 2

Note: Student samples are quoted verbatim and may contain spelling and grammatical errors.

Overview

The primary goals of the question were to assess a student's ability to (1) identify the experimental units, treatments, and response variable from a description of a completely randomized experimental design; (2) describe a correct procedure that could be used to randomly assign two treatments to the experimental units in a completely randomized design; and (3) describe the benefit of using random assignment in an experimental design.

This question primarily assesses skills in skill category 1: Selecting Statistical Methods and skill category 4: Statistical Argumentation. Skills required for responding to this question include (1.B) Identify key and relevant information to answer a question or solve a problem, (1.C) Describe an appropriate method for gathering and representing data, and (4.B) Interpret statistical calculations and findings to assign meaning or assess a claim.

This question covers content from Unit 3: Collecting Data of the course framework in the AP Statistics Course and Exam Description. Refer to topics 3.5 and 3.7 and learning objectives VAR-3.A, VAR-3.B, and VAR-3.E.

Sample: 2A Score: 4

The response earned the following: Part (a) - E; Part (b) - E; Part (c) - E.

In part (a) the response identifies the experimental units as driveways, the treatments are identified as concrete with fibers and concrete without fibers, and the response variable is identified as the severity of cracks. Because all three components are satisfied, part (a) was scored essentially correct (E). In part (b) the driveways are labeled 1 to 60. A random number generator is used to select 30 driveways from 1 to 60, ignoring repeats. This group is assigned to the concrete with fibers treatment, and the other 30 driveways are assigned to concrete without fibers. Component 1 is satisfied. The random process results in two treatment groups with the same number of driveways. Component 2 is satisfied. As both components are satisfied, part (b) was scored essentially correct (E). In part (c) the response states the developer "can conclude that the concrete with fibers is causing less driveway cracks." As both components are satisfied, part (c) was scored essentially correct (E).

Sample: 2B Score: 3

The response earned the following: Part (a) - E; Part (b) - P; Part (c) - E.

In part (a) the response identifies the experimental units as homes in need of driveways. The treatments are identified as concrete containing fibers and concrete not containing fibers, and the response variable is identified as the severity of cracks. Because all three components are satisfied, part (a) was scored essentially correct (E). In part (b) the driveways are labeled 1 to 60. The hat method is used to assign driveways to concrete with or without fibers. However, the response does not indicate that slips of paper were mixed first and does not state that the slips are selected without replacement. Component 1 is not satisfied. The random process results in two treatment groups of equal size. Component 2 is satisfied. As one of the two components is satisfied, part (b) was scored partially correct (P). In part (c) the response indicates the benefit of random assignment is that causation can be inferred. Component 1 is satisfied. The response is stated in context. Component 2 is satisfied. Because both components are satisfied, part (c) was scored essentially correct (E).

Question 2 (continued)

Sample: 2C Score: 2

The response earned the following: Part (a) – E; Part (b) – P; Part (c) – P.

In part (a) the response identifies the experimental units as homes that need new driveways, the treatments are identified as concrete that contains fibers and concrete that does not contain fibers, and the response variable is identified as the severity of cracks. Because all three components are satisfied, part (a) was scored essentially correct (E). In part (b) the houses are given a label between 1 and 60. A random number generator is used to generate 30 numbers from 1 to 60. The response does not indicate that duplicate numbers from the random number generator should be ignored. Component 1 is not satisfied. The random process results in an equal number of driveways with concrete containing fibers and with concrete not containing fibers. Component 2 is satisfied. Because one component is satisfied, part (b) was scored partially correct (P). In part (c) the response links random assignment to the reduction of confounding and mentions concrete with fibers. As the response discusses confounding in context, part (c) was scored partially correct (P).