# AP' Physics l: Algebra-Based Sample Student Responses and Scoring Commentary 

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Free-Response Question 3
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For the length of the arrow at $t=t_{2}$ being longer than the arrow at $t=t_{1}$

## Scoring Notes:

- A maximum of 1 point can be earned if extraneous unlabeled arrows are drawn.
- A maximum of 1 point can be earned if incorrect labeled forces are drawn.


## Example Response


(a)(ii) For an explanation that refers to the difference in the stretch length and indicates that the magnitude of the spring force is (or is not) related to the stretch length, consistent with the force diagram drawn in part (a)(i)

## Example Response

The spring force arrow drawn at $t=t_{2}$ is longer because the spring is stretched a greater distance at that time and the spring force is related to the stretch distance.
(a)(iii) For a correct selection with an attempt at a relevant justification, or a selection and
justification consistent with the response in part (a)(ii)
For indicating that the spring force is the net force $\mathbf{1}$ point
Scoring Note: Stating $F=k x$ earns this point.
For indicating that the net force is related to the speed (or acceleration) $\mathbf{1}$ point
Scoring Note: The relationship does not need to be defined to earn this point.

## Example Response

$$
\ldots v_{1}>v_{2} \quad \mathrm{X} v_{1}<v_{2} \quad v_{1}=v_{2}
$$

The net force is the spring force. When the spring is stretched a greater length, the spring force is greater, so the net force is greater, and therefore the tangential speed is greater at $t=t_{2}$.

Total for part (a) $\mathbf{6}$ points
(b)(i) For the correct answer: $F_{\text {net }}=k_{0} d \quad \mathbf{1}$ point

## Scoring Notes:

- An answer of $k x$ does not earn this point.
- Points for part (b)(i) may be earned if correct in (b)(ii).


## Example Response

$$
\begin{aligned}
& F_{\text {net }}=\Sigma F=F_{s} \\
& F_{\text {net }}=\Sigma F=k_{0} d
\end{aligned}
$$

(b)(ii) For a multistep derivation that begins with Newton's second law: $\Sigma F=m a \quad \mathbf{1}$ point

For one of the following:
1 point

- Substituting $k x$ for force into Newton's second law
- Substituting $\frac{v^{2}}{r}$ for acceleration into Newton's second law
- Substituting $(L+d)$ for the radius

For the consistent answer in terms of the given variables: $v=\sqrt{\frac{k_{0} d(L+d)}{m_{0}}}$

## Scoring Notes:

- Subscripts for $m$ and $k$ are not required to earn this point.
- Points in (b)(ii) can be earned if correct in (b)(i).


## Example Response

$$
\begin{aligned}
& \Sigma F=m a_{c} \\
& k x=\frac{m v^{2}}{r} \\
& k_{0} d=\frac{m_{0} v^{2}}{L+d} \\
& v=\sqrt{\frac{k_{0} d(L+d)}{m_{0}}}
\end{aligned}
$$

(c) For an answer that attempts to use functional dependence to relate the tangential speed with $\mathbf{1}$ point

Scoring Note: It is not necessary to use the functional dependence correctly to earn this point.

For a correct explanation for why the derived equation in part (b)(ii) does or does not $\mathbf{1}$ point support the reasoning in part (a)

## Example Response

My equation from part (b) (ii) agrees with my reasoning in part (a). The tangential speed of the block as it travels in a horizontal circle is related to the distance the spring is stretched. The greater the tangential speed of the block, the greater distance the spring is stretched. The equation shows this because the $d$ is in the numerator.

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## Question 3

## Continue your response to QUESTION 3 on this page.

i. On the following dots, which represent the block at the locations shown in Figure 1 and Figure 2, draw the force that is exerted on the block by the spring at times $t=t_{1}$ and $t=t_{2}$. The spring force must be represented by a distinct arrow starting on, and pointing away from, the dot.
Note; Draw the relative lengths of the vectors to reflect the relative magnitudes of the forces exerted by the spring at both times.

$t=t_{1}$

$t=t_{2}$
ii. Referencing $d_{1}$ and $d_{2}$, describe your reasoning for drawing the arrows the length that you did in part (a)(i).
$d_{2}>d_{1}$, so the spring at $t_{2}$ is stretched further and applies a greater Force compared to $t_{1}$ the further stretched spring at $t_{2}$ applies a greater force on the block, so the force on the black by the Spring is e grater and has a higher magnitude.
iii. Is the tangential speed $v_{1}$ of the block at time $t=t_{1}$ greater than, less than, or equal to the tangential speed $v_{2}$ of the block at time $t=t_{2}$ ?


$$
\ldots v_{1}=v_{2}
$$

Justify your answer without using equations.
When the tangential velocity of the block is greater, the centripetal

## P1 Q3 Sample 3A Page 3 of 3

## P1 Q3 Sample 3B Page 1 of 3

3. ( 12 points, suggested time 25 minutes)

A small block of mass $m_{0}$ is attached to the end of a spring of spring constant $k_{0}$ that is attached to a rod on a horizontal table. The rod is attached to a motor so that the rod can rotate at various speeds about its axis. When the rod is not rotating, the block is at rest and the spring is at its unstretched length $L$, as shown. All frictional forces are negligible.


Figure 1
Figure 2
(a) At time $t=t_{1}$, the rod is spinning such that the block moves in a circular path with a constant tangential speed $v_{1}$ and the spring is stretched a distance $d_{1}$ from the spring's unstretched length, as shown in Figure 1 . At time $t=t_{2}$, the rod is spinning such that the block moves in a circular path with a constant tangential speed $v_{2}$ and the spring is stretched a distance $d_{2}$ from the spring's unstretched length, where $d_{2}>d_{1}$, as shown in Figure 2.

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Question 3

Continue your response to QUESTION 3 on this page.
i. On the following dots, which represent the block at the locations shown in Figure 1 and Figure 2, draw the force that is exerted on the block by the spring at times $t=t_{1}$ and $t=t_{2}$. The spring force must be represented by a distinct arrow starting on, and pointing away from, the dot.
Note: Draw the relative lengths of the vectors to reflect the relative magnitudes of the forces exerted by the spring at both times.

$t=t_{1}$

$t=t_{2}$
ii. Referencing $d_{1}$ and $d_{2}$, describe your reasoning for drawing the arrows the length that you did in part (a)(i).
As He distance grows between He black and $L$ the spry pure will get weaker and weaker since At is further quay prom the center
iii. Is the tangential speed $v_{1}$ of the block at time $t=t_{1}$ greater than, less than, or equal to the tangential speed $\nu_{2}$ of the block at time $t=t_{2}$ ?
$\qquad$

$$
v_{1}>v_{2}
$$


$\nu_{1}<\nu_{2}$


Justify your answer without using equations.
Tingetial speed aprected by the elastance prom He center. Me is lew the distence the hoshe the rungetrent speed

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Page 11 GO ON TO THE NEXT PAGE.

Use a pencil or a per with black or dark blue ink. Do NOT write your name. Do NOT write outside the box.

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Question 3

Continue your response to QUESTION 3 on this page.
(b) Consider a scenario where the block travels in a circular path where the spring is stretched a distance $d$ from its unstretched length $L$.
i. Determine an expression for the magnitude of the net force $F_{\text {net }}$ exerted on the block. Express your answer in terms of $m_{0}, k_{0}, L, d$, and fundamental constants, as appropriate.

$$
\begin{aligned}
& \angle F=m g \quad \text { Fret }=m_{0} \frac{v^{2}}{r} \\
& \text { Fret } 2 \text { RN }_{m_{0}} \frac{\left(k L_{0} \cdot R N D^{2}\right.}{L-d} \\
& \text { Pret } 2 m_{0} \frac{\left(k_{0} \cdot F N^{2}\right)^{2}}{L^{-d}}
\end{aligned}
$$

ii. Derive an equation for the tangential speed $v$ of the block. Express your answer in terms of $m_{0}, k_{0}, L, d$, and fundamental constants, as appropriate.


$$
v=k_{0} \cdot f_{N}
$$

$$
K_{U} \cdot F N=\frac{F_{n e t} \cdot(L+d)}{M_{0}}
$$

(c) Does your equation for the tangential speed $v$ of the block from part (b)(ii) agree with your reasoning from part (a) ?

$\qquad$ No
Explain your reasoning.
As Labs in the nnecitor an means that on Anerease in the distmee wald achuill mereage the tangetal speed ap the block.

Use a pencil or a pen with black or dark blue ink. DO NOT write your name. DO NOT withe outside the box.

## Question 3

## Continue your response to QUESTION 3 on this page.

i. On the following dots, which represent the block at the locations shown in Figure 1 and Figure 2, draw the force that is exerted on the block by the spring at times $t=t_{1}$ and $t=t_{2}$. The spring force must be represented by a distinct arrow starting on, and pointing away from, the dot.
Note: Draw the relative lengths of the vectors to reflect the relative magnitudes of the forces exerted by the spring at both times.

$t=t_{1}$

$t=t_{2}$
ii. Referencing $d_{1}$ and $d_{2}$, describe your reasoning for drawing the arrows the length that you did in part (a)(i).
I drew the arrow for tension at $t=t$. smaller then $t=t_{r}$ because $d_{1}$ is smaller at $t=t$. meaning tension the block is $d_{2}$.
iii. Is the tangential speed $v_{1}$ of the block at time $t=t_{1}$ greater than, less than, or equal to the tangential speed $\nu_{2}$ of the block at time $t=t_{2}$ ?
$\qquad$

$\qquad$ $v_{1}=v_{2}$

Justify your answer without using equations.
The rod is spinning the block faster at $t_{2}$ manning that it has a grater velocity.

## Question 3

Note: Student samples are quoted verbatim and may contain spelling and grammatical errors.

## Overview

The responses were expected to demonstrate the ability to:

- Identify a net force in a given scenario.
- Compare relative magnitudes of the net force in two different scenarios.
- Relate force and spring length through functional dependence.
- Relate force and tangential velocity in a circular motion through functional dependence.
- Compare tangential velocities in two scenarios based on centripetal force/acceleration.
- Derive an expression for tangential velocity beginning with Newton's second law equation.
- Identify the net force as a centripetal force.
- Identify the functional dependence between stretch length of a rotating spring and tangential velocity.
- Determine consistency between reasoning based on a conceptual argument and a derived equation.


## Sample: 3A

Score: 12
Part (a)(i) earned 2 points. One point was earned for indicating two arrows drawn to the right. The second point was earned for indicating the length of the arrow at $t_{2}$ as longer than the arrow at $t_{1}$. Part (a)(ii) earned 1 point for stating, "the spring at $t_{2}$ is stretched further and applies a greater force compared to $t_{1}$." The length is related to the spring force. Part (a)(iii) earned 3 points. One point was earned for checking the correct selection, $v_{1}<v_{2}$, with an attempt to justify the selection. The second point was earned for identifying the force as the spring force by stating, " $[t]$ he greater force the spring applies to the block" and indicating the net force as the centripetal force. The third point was earned for stating, "When the tangential velocity of the block is greater, the centripetal acceleration and force will also be greater." Part (b)(i) earned 1 point for correctly identifying the net force expression with the correct variables substituted. Part (b)(ii) earned 3 points. One point was earned for attempting to use Newton's second law. The second point was earned for correctly substituting $L+d$ for the radius, and the third point was earned for giving the correct equation. Part (c) earned 2 points. One point was earned for indicating a functional dependence between velocity and distance by stating, "If $v$ increases, so does $d$, and vice versa." The second point was earned for correctly relating the equation from part (b) to the reasoning in part (a).

## Question 3 (continued)

## Sample: 3B

## Score: 7

Part (a)(i) earned 1 point for indicating two arrows drawn to the right. Extraneous arrows are labeled and correct. The second point was not earned because the response does not indicate the length of the arrow at $t_{2}$ is longer than the arrow at $t_{1}$. Part (a)(ii) earned 1 point for stating, "As the distance grows between the block and $L$ the spring force will get weaker and weaker." The length is related to the spring force. This is consistent with the arrows drawn in part (a)(i). Part (a)(iii) earned 1 point for checking the correct selection, $v_{1}<v_{2}$, with an attempt to justify the selection. The second point was not earned because the response does not identify the spring force as the net force. The third point was not earned because the response does not show a relationship between the spring force and the velocity. Part (b)(i) earned no points because the response does not give a correct expression for the net force. Part (b)(ii) earned 2 points. One point was earned for attempting to use Newton's second law. The second point was earned for correctly substituting $\frac{v^{2}}{r}$ for the centripetal acceleration, and the third point was not earned because the response did not give the correct equation. Part (c) earned 2 points. One point was earned for attempting to express a functional dependence between velocity and distance by stating, "an increase in the distance would actually increase the tangential speed of the block." The second point was earned for correctly relating the equation in part (b) to support the reasoning in part (a). The response states, "As $L+d$ is in the numerator it means that an increase in the distance would actually increase the tangential speed."

## Sample: 3C

## Score: 5

Part (a)(i) earned 2 points. One point was earned for indicating two arrows pointing to the right, and the other point was earned for indicating the arrow for $t_{1}$ is shorter than the arrow for $t_{2}$. Extraneous forces are labeled and correct. Part (a)(ii) earned 1 point for stating, "I drew the arrow for tension at $t=t_{1}$ smaller than $t=t_{2}$ because $d_{1}$ is smaller." The force (tension) is related to the stretch. Part (a)(iii) earned 1 point for checking the correct selection, $v_{1}<v_{2}$, and attempting a relevant justification. The second point was not earned because the response does not identify the spring force as the net force. The third point was not earned because the response does not show a relationship between the spring force and the velocity. Part (b)(i) earned no points because the response does not give a correct expression for the net force. Part (b)(ii) earned 1 point for correctly substituting $(L+d)$ for the radius. The second point was not earned because the response does not start with Newton's second law, and the third point was not earned because the response does not give the correct equation. Part (c) earned no points. The first point was not earned because the response does not attempt to show a functional dependence between velocity and stretch length. The second point was not earned because the response does not attempt to relate the equation in part (b) to support the reasoning in part (a).

